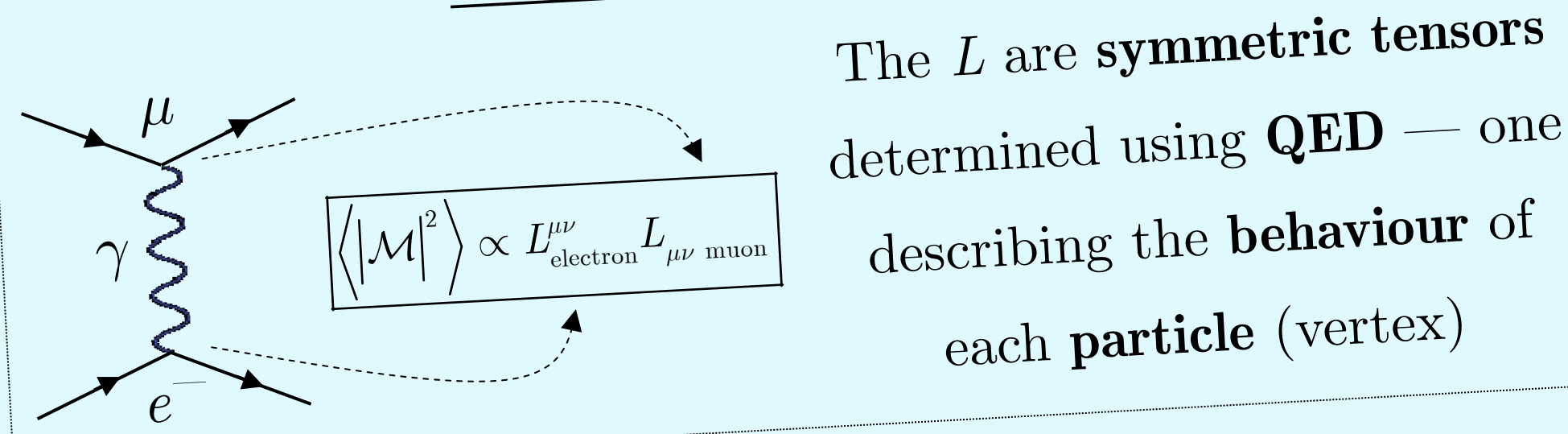


3 Scattering Cross-Sections

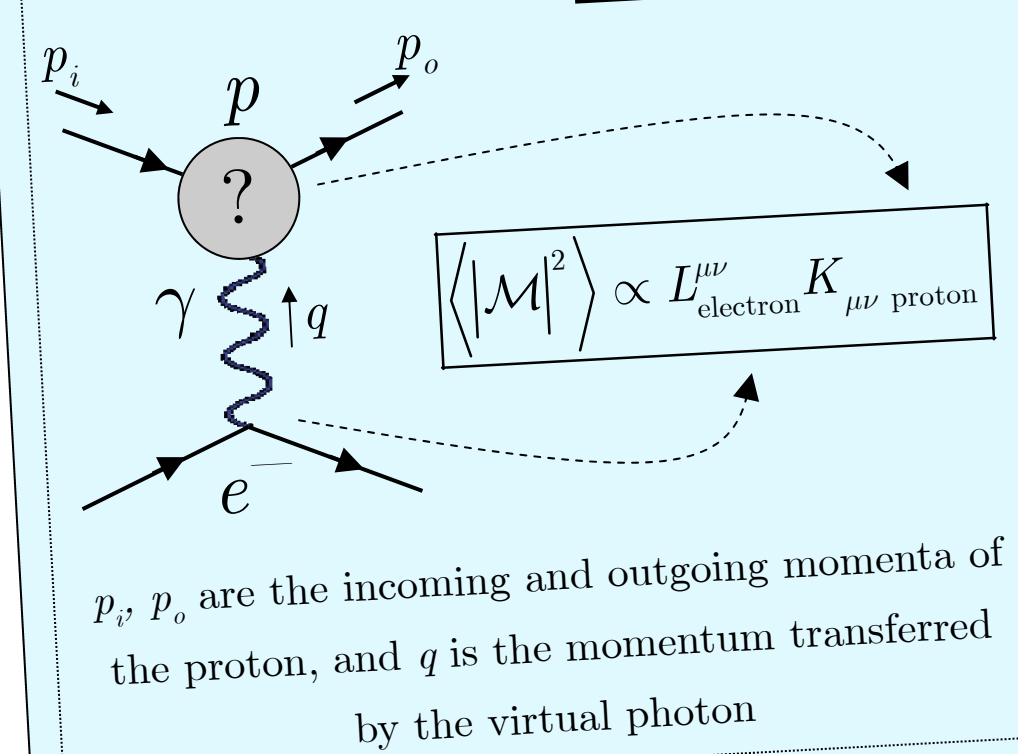
~ Spin Averaged Amplitudes ~

Electron-Muon Scattering



The L are symmetric tensors determined using QED — one describing the behaviour of each particle (vertex)

Electron-Proton Scattering



For elastic scattering, L_{electron} remains as before. K_{proton} encodes the (unknown) way the proton behaves. This depends on the form factors.

p_i, p_o are the incoming and outgoing momenta of the proton, and q is the momentum transferred by the virtual photon

~ Form Factors ~

- K is not completely unknown:
 - It must be symmetric (since $L^{\mu\nu}$ is symmetric)
 - It can only depend on q, p_i and p_o , and $q = p_o - p_i$.
- Mathematically, there are only so many ways of obtaining a symmetric tensor from only two four-vectors. $K_{\mu\nu}$ can only contain two independent numbers — say K_1 and K_2 .
- We then obtain the famous Rosenbluth Formula:

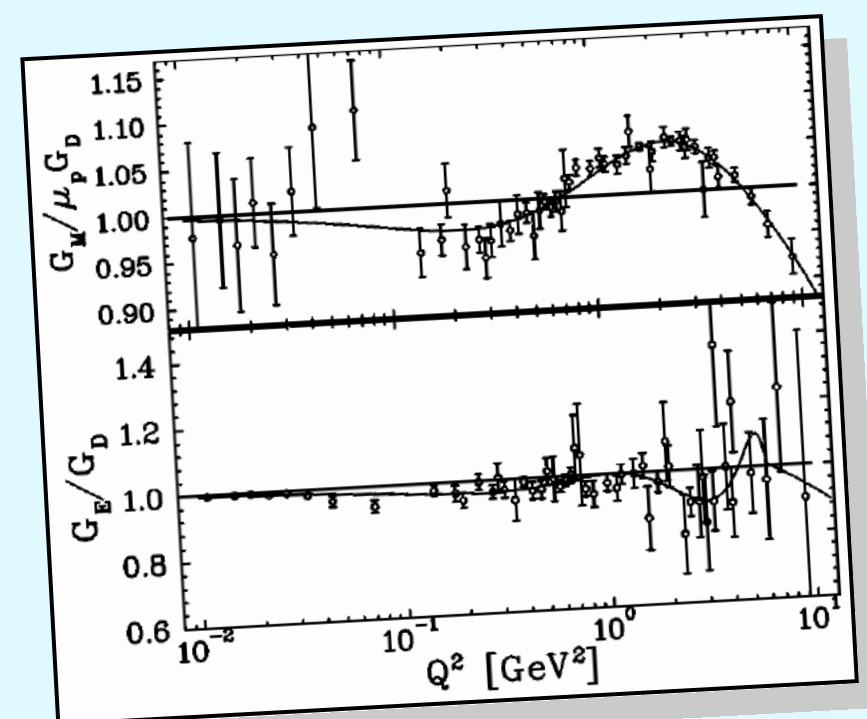
$$\frac{d\sigma}{d\Omega} = \left(\frac{\alpha}{4m_p E \sin^2(\theta/2)} \right)^2 \frac{E'}{E} \left[2K_1 \sin^2(\theta/2) + K_2 \cos^2(\theta/2) \right]$$

Labels: Fine structure const. α , Incident energy of electron E , Scattering angle θ , Proton mass m_p , Outgoing energy of electron E' .

- By experimentally measuring cross sections at fixed q for a range of angles and energies, we can determine K_1 and K_2 . By carrying out these measurements at a range of q , we find the functions $K_1(q)$ and $K_2(q)$.
- These are sufficient to determine the form factors

$$K_1 = -q^2 G_M^2 \quad K_2 = (2m_p)^2 \frac{(2m_p)^2 G_E^2 - q^2 G_M^2}{(2m_p)^2 - q^2}$$

~ Results ~



J. Arrington, Phys. Rev. C 69, 022201(R) (2004).

Current data indicates that both electric and magnetic form factors have the same dipole distributions G_D :

$$\frac{G_E}{G_D} = \frac{G_M}{\mu G_D} = 1$$

Such form factors indicate that charge is concentrated in the centre of the proton, and decreases exponentially.

OLYMPUS

8.276 Final Poster — Daniel Guetta — guetta@cantab.net

2 Theory

- In theory, if we know everything about the proton, we should be able to obtain an analytic expression for the form factors.
- Advances in lattice QCD techniques are getting us closer and closer to this goal, and results are expected in the foreseeable future...
- In the meantime, however, theorists can't help much.

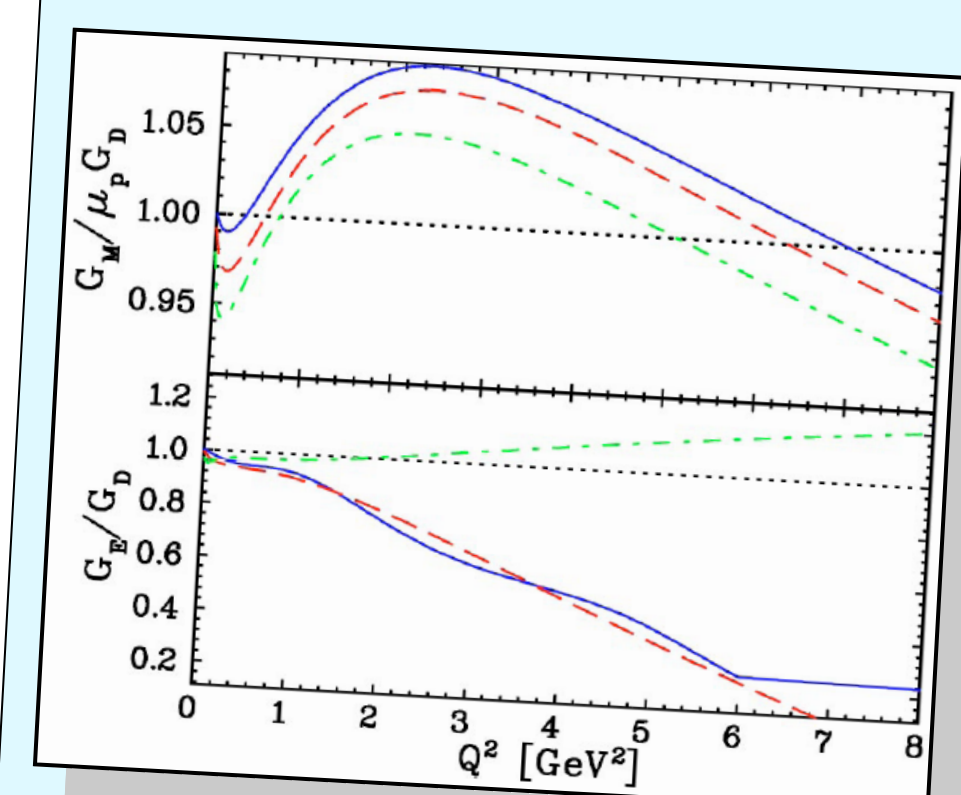
Polarised Scattering

- The factors G_E and G_M can also be determined by performing scattering experiments using polarised particles.
- For example when polarised electrons are scattered off unpolarised protons, polarisation transfer occurs to the proton with two components — parallel (P_{\parallel}) and perpendicular (P_{\perp}) to the proton momentum in the scattering plane. In fact:

$$\frac{G_E}{G_M} = -\frac{P_{\perp}}{P_{\parallel}} \frac{(E + E')}{2m_p} \tan\left(\frac{\theta}{2}\right)$$

- Similarly, carrying out e^-p scattering with spins aligned and anti-aligned and measuring the difference in cross sections (the scattering asymmetry) allows us to determine the form factors.
- A crucial aspect of these experiments is that they only occur when a single photon is transferred in the interaction.

~ Results ~



J. Arrington, Phys. Rev. C 69, 022201(R) (2004).

Green: cross section measurements
Red/blue: polarisation measurements

These form factors predict a much richer inner structure.

Measurements using these method produce roughly similar results for G_M but completely different results for G_E . Something has gone awry. The measurements even predicts a node in G_E near 8 (GeV/c)^2 .

1 Introduction

- The electric and magnetic form factors, G_E and G_M describe the distribution of "stuff" in the proton.
- There are a number of ways to measure these, which, to date, have led to inconsistent results.
- The current theory is that cross-section measurements are contaminated by two-photon processes.
- OLYMPUS will attempt to ascertain to what extent this is true.

Practical Details

- Measurements of this kind have already been made, but at low energy (~ 500 MeV) and with poor precision. The aim of OLYMPUS is to make measurements in the 2 GeV range with 1% precision.

~ Getting the Particles ~



DESY Website

The experiment will use the DORIS storage ring at DESY in Hamburg, Germany. Because (1) it can be used to store both e^- and e^+ at high energies and (2) the beams can be switched from e^+ to e^- in under an hour. The experiment would involve installing an unpolarised hydrogen gas target at the storage ring.

~ Detecting the results ~



The experiment will use the BLAST (Bates Large Acceptance Spectrometer Toroid) detector from the MIT-Bates accelerator.

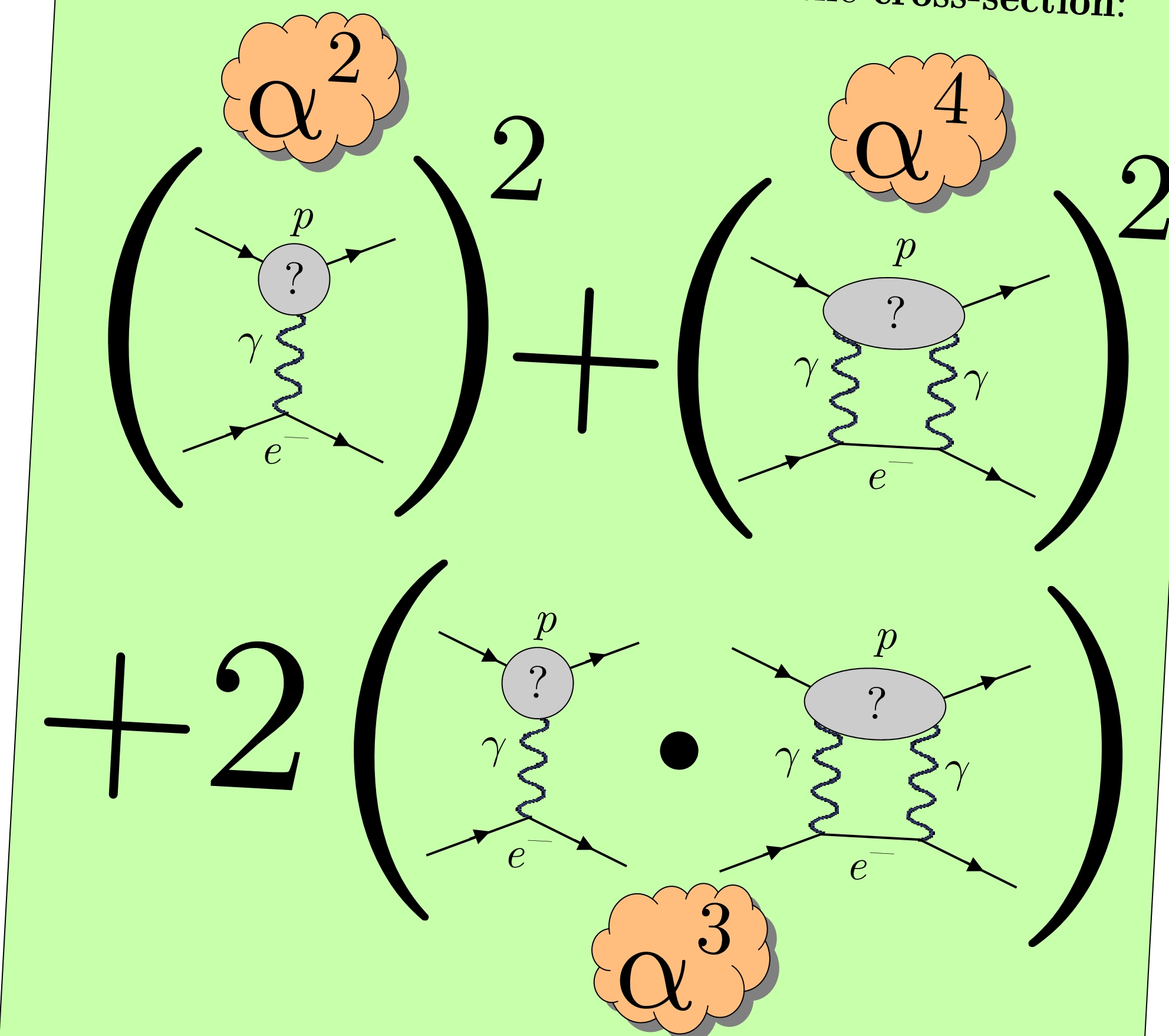
It is optimally designed for 1-2 GeV elastic ep scattering because of its toroidal shape (the beam can be located in the centre of the detector) and its drift chambers. Only problem — it's over 3500 miles away!

Explanation

- A crucial assumption in deriving the Rosenbluth Formula was that the Born approximation applied (ie: only one photon was involved in the interaction).
- Polarisation transfer only occurs in one-photon processes, and does not rely on this approximation.
- The idea is that the cross-section measurements are polluted by second-order interactions. These render the resulting form-factors meaningless, because the entire (already doubtful) interpretation of these measurements as fourier transforms of the charge distribution relies heavily on the assumptions that only single-photon processes are involved.

Proving it!

- Assuming second-order processes occur, three terms will appear in the ep scattering cross-section: one arising purely from single-photon processes, one from purely multi-photon processes and one from the interference of these two processes.
- Each vertex adds one power of the fine-structure constant to the cross section. Thus, each term contributes a different power of α to the cross-section:



- Using a positron is effectively equivalent to time reversal in the electron vertices, and QED tells us that this reverses the sign of the coupling constant α .
- This makes the third term flip sign.
- We can therefore measure the importance of second-order interactions by measuring the difference in cross-section between e^-/p and e^+/p scattering.

Many thanks to Prof R. Milner for the help and support he so kindly and willingly provided in helping me prepare this poster, and to Prof J. Conrad and E. Sfakianakis for their help throughout 8.276.